(only B is put into solution)

For a weak base (B) in water:

$$B + H_2O \rightleftharpoons OH^- + BH^+$$

$$K_{\rm b} = \frac{[\rm OH^-][\rm BH^+]}{[\rm B]}$$

and let $C_{\rm B}$ be the analytical concentration (label) of the weak base

Our Equilibrium "ICE" Table

	[B]	[OH ⁻]	[BH⁺]
initial	C_{B}	0	0
change	- <i>x</i>	+ <i>x</i>	+ <i>x</i>
equilibrium	$C_{\rm B}-x$	x	x

$$K_{\rm b} = \frac{x^2}{(C_{\rm B} - x)}$$
 Equation 1.1

$$K_{\rm b}C_{\rm B} - K_{\rm b}(x) = x^2$$

$$0 = x^2 + K_{\rm b}(x) - K_{\rm b}C_{\rm B}$$

$$[OH^-] = [BH^+] = x = \frac{-K_{\rm b} + \sqrt{K_{\rm b}^2 + 4K_{\rm b}C_{\rm B}}}{2}$$

This equation is the <u>exact</u> solution for calculating the [OH⁻] for any solution made by mixing a concentration of ONLY a weak base in water. (What I have designated a "Type 1" problem)

If we are using a REASONABLE concentration for B (somewhere between 1.0 M and 0.05 M) AND K_b is small enough (say less than 10⁻⁴) we can make the following assumption:

 $C_{\rm B} - x \cong C_{\rm B}$ all this is saying is that x is so small compared to $C_{\rm B}$, it doesn't change it

So that Equation 1.1 shown above becomes

$$K_{\rm b} = \frac{x^2}{\rm C_{\rm B}}$$

and solving:

$$[OH^-] = [BH^+] = x = \sqrt{K_b C_B}$$
 Equation 1.2

This equation is the <u>approximate</u> solution for calculating the $[OH^-]$ for any weak base with $K_b < 10^{-4}$ when put in water.