## Worksheet 3

1. Isopropyl alcohol can dissociate into acetone and hydrogen:
$\left(\mathrm{CH}_{3}\right) \mathrm{CHOH}(\mathrm{g}) \leftrightharpoons\left(\mathrm{CH}_{3}\right) \mathrm{CO}(\mathrm{g})+\mathrm{H}_{2}(\mathrm{~g})$
At $179{ }^{\circ} \mathrm{C}$, the equilibrium constant for this dehydrogenation reaction is 0.444 .
(a) If 10.00 g of isopropyl alcohol is placed in a 10.00 L vessel and heated to $179^{\circ} \mathrm{C}$, what is the partial pressure of acetone when equilibrium is attained?
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\(\mathrm{T}=179^{\circ} \mathrm{C}=452 \mathrm{~K}\)
\(K=0.444\)
\(\mathrm{m}=10 \mathrm{~g} \times 1 \mathrm{~mol} / 60 \mathrm{~g}=0.167 \mathrm{~mol}\left(\mathrm{CH}_{3}\right) \mathrm{CHOH}\)
\(\mathrm{V}=10.0 \mathrm{~L}\)
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$\mathbf{P}=\mathrm{nRT} / \mathrm{V}=(\mathbf{0 . 1 6 7} \mathrm{mol})\left(\mathbf{0 . 0 8 2 0 6} \mathrm{atm} \mathrm{L} \mathrm{mol}{ }^{-1} \mathrm{~K}^{-1}\right)(452 \mathrm{~K}) / 10.0 \mathrm{~L}$
$P_{(C H 3) 2 \mathrm{CHOH}}=0.619 \mathrm{~atm}$
$\left(\mathrm{CH}_{3}\right) \mathrm{CHOH}(\mathrm{g}) \leftrightharpoons\left(\mathrm{CH}_{3}\right) \mathrm{CO}(\mathrm{g})+\mathrm{H}_{2}(\mathrm{~g})$

| initial $P$ | 0.619 atm | 0 | 0 |
| :--- | :--- | :--- | :--- |
| $\Delta P$ | $-\mathbf{x}$ | $+\mathbf{x}$ | $+\mathbf{x}$ |
| equilibrium $P$ | $\mathbf{0 . 6 1 9}-\mathrm{x}$ | $\mathbf{x}$ | $\mathbf{x}$ |

$\mathbf{( 0 . 4 4 4 )}=\mathrm{x}^{2} /(\mathbf{0 . 6 1 9 - x})$
0.275-0.444x $=x^{2}$
$x^{2}+0.444 x-0.275=0$, solve using the Quadratic formula
$x=\left(-0.444 \pm \sqrt{ }(.444)^{2}-4(1)(0.275)\right) / 2=0.347 \mathrm{~atm}=P_{\text {acetone }}$
(b) What fraction of isopropyl alcohol is dissociated at equilibrium?

The actual $P_{\text {isopropyl alcohol }}=0.619 \mathrm{~atm}-0.347 \mathrm{~atm}=0.272 \mathrm{~atm}$
The fraction of dissociated isopropyl alcohol $=(\mathbf{0 . 6 1 9})(0.272) / 0.619=0.562$
2. The equilibrium constant for the reaction:
$\mathrm{H}_{2}(g)+\mathrm{I}_{2}(s) \leftrightharpoons 2 \mathrm{HI}(g)$
at $25^{\circ} \mathrm{C}$ is $\mathrm{K}=0.345$.
(a) If the partial pressure of hydrogen is $\mathrm{P}_{\mathrm{H} 2}=1.00 \mathrm{~atm}$ and solid iodine is present, what is the equilibrium partial pressure of hydrogen iodide, $\mathrm{P}_{\mathrm{HI}}$, at $25^{\circ} \mathrm{C}$ ?
$P_{H 2}=1.00 \mathrm{~atm}$
$\mathrm{K}=0.345$
$\mathrm{K}=\left(\mathbf{P}_{\mathrm{HI}}\right)^{\mathbf{2}} /\left(\mathbf{P}_{\mathrm{H} 2}\right)$
$0.345=\left(\mathrm{P}_{\mathrm{HI}}\right)^{2} /(1.00 \mathrm{~atm})$
$\mathrm{P}_{\mathrm{HI}}=0.587 \mathrm{~atm}$

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(b) An excess of solid $\mathrm{I}_{2}$ is added to a container filled with hydrogen at $25^{\circ} \mathrm{C}$ and a pressure of 4.00 atm . Calculate the pressures of $\mathrm{H}_{2}(\mathrm{~g})$ and $\mathrm{HI}(\mathrm{g})$ reached at equilibrium.

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\mathrm{H}_{2}(\mathrm{~g})+\mathrm{I}_{2}(\mathrm{~s}) \leftrightharpoons 2 \mathrm{HI}(\mathrm{~g})
$$

| initial $P$ | 4.00 atm | 0 | 0 |
| :--- | :--- | :--- | :--- |
| $\Delta P$ | $-x$ | 0 | $2 x$ |
| equilibrium $P$ | $4.00-x$ | 0 | $2 x$ |

$(0.345)=2 \mathrm{x}^{2} /(4.00-\mathrm{x})$
$1.38-0.345 \mathrm{x}=4 \mathrm{x}^{2}$
$4 x^{2}+0.345 x-1.38=0$, solve using the Quadratic formula
$x=\left(-0.345 \pm \sqrt{ }(.345)^{2}-4(4)(1.38)\right) / 8=0.546 \mathrm{~atm}$
$\mathrm{P}_{\mathrm{H} 2}=4.00 \mathrm{~atm}-0.546 \mathrm{~atm}=3.45 \mathrm{~atm}$
$\mathrm{P}_{\mathrm{HI}}=\mathbf{2 x}=1.09 \mathrm{~atm}$
3. At $300^{\circ} \mathrm{C}$ the equilibrium constant for the reaction
$\mathrm{PCl}_{5}(\mathrm{~g}) \leftrightharpoons \mathrm{PCl}_{3}(\mathrm{~g})+\mathrm{Cl}_{2}(\mathrm{~g})$
is $\mathrm{K}=11.5$.
(a) Calculate the reaction quotient $Q$ if initially $\mathrm{P}_{\mathrm{PCL} 3}=2.0 \mathrm{~atm}, \mathrm{P}_{\mathrm{C} 12}=6.0 \mathrm{~atm}$, and $\mathrm{P}_{\mathrm{PC} 15}$ $=0.10 \mathrm{~atm}$. State whether the reaction proceeds to the right or to the left as equilibrium is approached.
$\mathrm{K}=11.5$
$\mathrm{T}=300^{\circ} \mathrm{C}=\mathbf{5 7 3} \mathrm{K}$
$P_{\text {PCL } 3}=2.0 \mathrm{~atm}, \mathrm{P}_{\mathrm{C} 12}=6.0 \mathrm{~atm}$, and $\mathrm{P}_{\mathrm{PC} 15}=0.10 \mathrm{~atm}$
$\left.Q=\left(\mathbf{P}_{\mathrm{PCl} 3}\right)\left(\mathrm{P}_{\mathrm{C} 13}\right) / \mathbf{P}_{\mathrm{PC} 15}=\mathbf{( 2 . 0 )}\right)(\mathbf{6 . 0}) / \mathbf{0 . 1 0}=\mathbf{1 2 0}$
$Q>K$, the reaction proceeds toward the left (reactants)
(b) Calculate $\mathrm{P}_{\mathrm{PC} 1}, \mathrm{P}_{\mathrm{C} 12}$, and $\mathrm{P}_{\mathrm{PC} 15}$, at equilibrium.

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\mathrm{PCl}_{5}(\mathrm{~g}) \leftrightharpoons \mathrm{PCl}_{3}(\mathrm{~g})+\mathrm{Cl}_{2}(\mathrm{~g})
$$

| initial $P$ | 0.10 atm | 2.0 atm | 6.0 atm |
| :--- | :--- | :--- | :--- |
| $\Delta \mathrm{P}$ | +y | -y | -y |
| equilibrium P | $\mathbf{0 . 1 0}+\mathrm{y}$ | $2.0-\mathrm{y}$ | $\mathbf{6 . 0}-\mathrm{y}$ |

$K=\left(\mathbf{P}_{\mathrm{C} 13}\right)\left(\mathbf{P}_{\mathrm{C} 12}\right) / \mathbf{P}_{\mathrm{PCC} 15}=(\mathbf{2} .0-\mathbf{y})(\mathbf{6 . 0}-\mathbf{y}) /(\mathbf{0 . 1 0}+\mathbf{y})=\mathbf{1 1 . 5}$
$1.15+1.15 y=12.0-8.0 y+y^{2}$
$y^{2}-19.5 y+10.85=0$, solve using the Quadratic formula
$y=\left(19.5 \pm \sqrt{ }(19.5)^{2}-4(1)(10.85)\right) / 2=0.573 \mathrm{~atm}$
$\mathrm{P}_{\mathrm{PC} 15}=0.10 \mathrm{~atm}-0.573 \mathrm{~atm}=0.673 \mathrm{~atm}$

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$P_{\text {PC13 }}=2.0 \mathrm{~atm}-0.573 \mathrm{~atm}=1.427 \mathrm{~atm}$
$P_{C 12}=6.0 \mathrm{~atm}-0.573 \mathrm{~atm}=5.427 \mathrm{~atm}$
(c) If the volume of the system is then increased, will the amount of $\mathrm{PCl}_{5}$ present increase or decrease?

The increase in volume causes the reaction to shift to the side having more moles of gas. Thus, the amounts of PCl 5 will decrease.
4. At $1000 \mathrm{~K}, \mathrm{~K}_{\mathrm{p}}=19.9$ for the reaction $\mathrm{Fe}_{2} \mathrm{O}_{3}(s)+3 \mathrm{CO}(g) \leftrightharpoons 2 \mathrm{Fe}(s)+3 \mathrm{CO}_{2}(g)$. What are the equilibrium partial pressures of CO and $\mathrm{CO}_{2}$ if CO is the only gas present initially, at a partial pressure of 0.978 atm ?

$$
\mathrm{Fe}_{2} \mathrm{O}_{3}(\mathrm{~s})+3 \mathrm{CO}(\mathrm{~g}) \leftrightharpoons 2 \mathrm{Fe}(\mathrm{~s})+3 \mathrm{CO}_{2}(g)
$$

| initial $P$ | 0.978 atm | 0 atm |
| :--- | :---: | :--- |
| $\Delta P$ | $-\mathbf{3 x}$ | $+3 x$ |
| equilibrium $P$ | $0.978-3 x$ | $\mathbf{3 x}$ |

$K_{p}=\left(P_{\mathrm{CO} 2}\right)^{3} /\left(P_{\mathrm{CO}}\right)^{3}=19.9=(3 \mathrm{x})^{3} /(0.978-3 \mathrm{x})^{3}$, take the cube root of both sides to solve for $x$
${ }^{3} \sqrt{ } 19.9=2.71=3 x /(0.978-3 x)$
2.65-8.13x $=3 x$
$2.65=11.13 x$
$\mathrm{x}=2.65 / 11.13=0.238 \mathrm{~atm}$
$P_{C O}=0.978-3 x=0.978-3(0.238)=0.264 \mathrm{~atm}$
$\mathbf{P}_{\mathrm{CO} 2}=3 \mathrm{x}=3(0.238)=0.714 \mathrm{~atm}$
5. In the gas phase at $400^{\circ} \mathrm{C}$, isopropyl alcohol decomposes to acetone, an important industrial solvent:
$\left(\mathrm{CH}_{3}\right)_{2} \mathrm{CHOH}(\mathrm{g}) \leftrightharpoons\left(\mathrm{CH}_{3}\right)_{2} \mathrm{CO}(\mathrm{g})+\mathrm{H}_{2}(\mathrm{~g}) \quad \Delta \mathrm{H}=+57.3 \mathrm{~kJ}$
Does the amount of acetone increase, decrease, or remain the same when an equilibrium mixture of reactants and products is subjected to the following changes?
(a) The temperature is increased

An endothermic reaction shifts to the right as the temperature increases. The amount of acetone increases.
(b) The volume is increased

Because there is $\mathbf{1 ~ m o l ~ o f ~ g a s ~ o n ~ t h e ~ l e f t ~ s i d e ~ a n d ~} 2 \mathrm{~mol}$ of gas on the right side of the balanced equation, the stress of an increase in volume (decrease in pressure) is

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relieved by a shift in the reaction to the side with the larger number of moles of gas (in this case, to products). The amount of acetone increases.
(c) The addition of Argon

The addition of Ar (an inert gas) with no volume change does not affect the composition of the equilibrium mixture. The amount of acetone does not change.
(d) $\mathrm{H}_{2}$ is added
$\mathrm{H}_{2}$ (product) added; the amount of acetone decreases.
(e) A catalyst is added

A catalyst does not affect the composition of the equilibrium mixture. The amount of acetone does not change.

