

Chapter 4 – Which Sections for the Exam?

Chapter 4: Sections 1-12, 15, 17. You can skip sections 13, 14, and 16. However, you DO need to know the very first part of section 13 – specifically page 145.

Fundamentals

Know how to calculate molar mass. Know your nomenclature (still). Be able to calculate amounts of reactants or products when given amounts of reactant or products – this is called stoichiometry – KNOW IT. Know how to determine the limiting reactant and how much product it leads to. Be able to incorporate percent yield into a problem if necessary.

How to measure pressure

Know the basics of how a manometer works and how a barometer works. Know how to calculate the pressure due to a standing column of liquid:

$$P = dhg \quad (\text{see page 128})$$

Watch your units here. Pressure will be in pascals if you use kg/m^3 for density, and m for height. If the column is mercury, just get the height in mm and you've now got torr.

Gas Laws

Know the NAMES and the law associated with each name (scientist).

Boyle's Law: Pressure is inversely proportional to volume (assuming constant temperature and amount of gas, moles). Any units will work here.

$$P \propto 1/V \quad P_1V_1 = P_2V_2 = \text{constant}$$

Charles' Law: Volume is directly proportional to *absolute* temperature (assuming constant pressure and amount of gas, moles). Any units for volume but remember, T must be Kelvin.

$$V \propto T \quad \frac{V_1}{T_1} = \frac{V_2}{T_2} = \text{constant}$$

Avogadro's Law: Volume is directly proportional to amount of gas in moles. (assuming constant temperature and pressure).

$$V \propto n \quad \frac{V_1}{n_1} = \frac{V_2}{n_2} = \text{constant}$$

Combined Gas Law: Most books and people refer to this as Boyle's Law + Charles' Law which is

$$\frac{P_1V_1}{T_1} = \frac{P_2V_2}{T_2} \quad (\text{assuming constant } n)$$

However, our book throw's in Avogadro's Law also giving:

$$\frac{P_1V_1}{n_1T_1} = \frac{P_2V_2}{n_2T_2} = \text{constant}$$

which is fine, except that this is really just the

Ideal Gas Law in disguise. The constant that is defined by this version of the combined gas law is the Universal Gas constant, R . So by definition:

$$R = \frac{PV}{nT} \quad \text{which rearranges to give}$$

$$PV = nRT$$

which is the **Ideal Gas Law** we all know and love.

When you use the ideal gas law be sure and use the right units on P , V , n , and T . You have no choice on n and T , they must be in moles and kelvin. Now you've got choices for units on P and V and THAT's why we've got 5 different values (OK, mostly different) of R listed in the back cover of our book. Here are my favorites (feel free to find one as your favorite):

$$R = 0.08206 \frac{\text{L}\cdot\text{atm}}{\text{mol}\cdot\text{K}} \quad \text{the old trusty L}\cdot\text{atm one}$$

$$R = 8.314 \frac{\text{kPa}\cdot\text{L}}{\text{mol}\cdot\text{K}} \quad \text{or} \quad \frac{\text{Pa}\cdot\text{m}^3}{\text{mol}\cdot\text{K}} \quad \text{the SI unit one}$$

$$R = 62.36 \frac{\text{L}\cdot\text{torr}}{\text{mol}\cdot\text{K}} \quad \text{the torr one comes in handy}$$

You might notice that these all just differ by the unit factors for pressure conversions. Like

$$0.08206 \times 760 = 62.36$$

See, it's not so bad. But I know what you're thinking. Do I (state your name) need to memorize all those values of R ? Why not? Drop that value of R into your next conversation and watch your popularity skyrocket. Oh well, I'll still print those values on the cover sheet to the exam for you to refer to while your brain is slowly melting.

STP SATP

A standard is whatever you chose as standard. Sometimes we chose different standards – and yes, I think that defeats the point in the first place but there you go. Know the difference in STP and SATP.

Let's MIX it up a bit

All those laws are great and work really well for most gases at reasonable pressures and temperatures. You can even apply those laws to mixtures of gases and just treat the whole mix as one big family of gas - that is you COUNT ALL the moles regardless of the type. When you do this you are calculating TOTAL pressure due to ALL the gases present. After you do that, I'm still going to want to know what the pressure is for each individual gas. The pressure exerted by say helium in a mixture of helium, neon, and xenon is the partial pressure of helium, P_{He} . Now the big lesson (and name!),

Dalton's Law of Partial Pressures: The total pressure of a system is equal to the sum of all the partial pressures within the system. Mathematically:

$$P_{\text{total}} = P_A + P_B + P_C + \dots$$

Now also realize that each of those partial pressures will have it's own version of the ideal gas law. What I mean is that $P_A V = n_A RT$. See, I'm only counting moles of A in this equation and I therefore get out P_A . One of the other neat results of this law is that partial pressure's ratio to the total pressure exactly match mole fractions. Uh-oh, what's a mole fraction? The number of moles of A divided by the total moles of gas in the mixture. Mole fraction of A is given by the symbol x_A (OK, so it's χ_A in the book – much too Greek for me). So by definition:

$$x_A = \frac{\text{mol A}}{\text{mol A} + \text{mol B} + \text{mol C} + \dots}$$

and you can set that equal to the pressure ratios:

$$x_A = \frac{P_A}{P_{\text{total}}} \quad \text{and therefore} \quad P_A = x_A P_{\text{total}}$$

So you can use pressures to get mole fractions OR use mole fractions to get pressures. Cool.

The confusion on effusion

Effusion of a gas is when a gas slips through a very small hole (or holes) from a high pressure to a low pressure. This IS what is going on when your once large and buoyant helium balloon is now much smaller and riding around on the floor. Helium effuses through the pores of the latex balloon. How fast does the helium effuse? Graham knows.

Graham's Law of Effusion: At constant temperature, the rate of effusion of a gas is inversely proportional to the square root of its molar mass.

$$\text{rate of effusion} \propto 1/\sqrt{M}$$

and so if you compare two gases at the same temperature you'll get

$$\frac{\text{rate of effusion of A}}{\text{rate of effusion of B}} = \sqrt{\frac{M_B}{M_A}}$$

The same exactly relation works for average speed also.

Temperature has the same square root dependence, but it is directly proportional to the rate of effusion or speed. For a given molar mass at two different temperatures:

$$\frac{\text{rate of effusion (or speed) at } T_2}{\text{rate of effusion (or speed) at } T_1} = \sqrt{\frac{T_2}{T_1}}$$

You can now combine the two affects of mass and temperature and get

$$\text{rate of effusion (or speed)} \propto \sqrt{\frac{T}{M}}$$

This can be set to an equality with a little work. YOU, however cannot worry about the work (shown on pages 146-147) and just look at the equation:

$$v_{\text{rms}} = \left(\frac{3RT}{M} \right)^{1/2}$$

Where v_{rms} is the root mean square speed.

You don't know how it feels – to be me

Ah yes, Tom Petty sang it so well and he never realized just how much all the real gases love that song. How DOES it feel to be real? Well for starters, you've got a real volume your OWNself. Real gas molecules DO have real diameters and take up space – ideal gases do NOT have a real diameter – they are just a point in space. Speaking of point, Tom Petty says in the same song, "let's get to the point..." See he was talking about ideal gases right? Actually, now that I think about it, and sing the rest of that chorus... he's talking about a whole other gas. But WAIT! Yes, he IS talking about real gases now that I think about it! Another line, "... think of me what you will, I've got a little space to fill". SEE? That's what gases do – fill space. I digress.

A great way to show non-ideality is too calculate a gas's actual (real) molar volume, V_m , and compare it to the molar volume of an ideal gas, V_m^{ideal} . When compared as a ratio, you get the compression factor, Z .

$Z = \frac{V_m}{V_m^{ideal}}$ this value of Z is typically plotted against pressure (see page 150, Figure 4.29). A negative value of Z corresponds to attractive forces being dominant. A positive value of Z corresponds to repulsive forces being dominant. Note that as zero pressure is approached, all real gases take on ideal behavior. Real gases aren't that far off the line at 1 atm either, which is why the ideal gas law works so well most of the time.

How to improve on an already IDEAL equation?

Once you decide you want an equation that really predicts well for real gases you got a choice between 2 basic equations. Both of which, "tweak" the ideal gas law into a real gas law. The main problem is that you must PICK the real gas you want the "law" to work for. All gases are NOT the same in the real world of gases, especially at high pressures and low temperatures – that is where the ideal gas law is at it's worst. So your choices are...

The Virial Equation:

$$PV = nRT \left(1 + \frac{B}{V_m} + \frac{C^2}{V_m^2} + \dots \right)$$

Now what you have here is a fixed up ideal gas law with 2 virial coefficients B and C . You have to get a new B and C for every gas at every temperature – yes, they are temperature dependent. So it works really well but it is a pain to use. Plus, I can't tell you what B and C mean in any physical or chemical sense – they are numbers that make the equation work well (think: curve fitting).

The van der Waals equation:

$$\left(P + a \frac{n^2}{V^2} \right) (V - nb) = nRT$$

Now we've got a fixed up equation but this time the two new variables are a and b . These are the van der Waals parameters and they are NOT temperature dependent – yea! You DO need to look up the values for a and b for every gas you want to work with though. The parameter a is an "adjustment" for attractive forces between molecules. The parameter b is like a volume correction term – it is roughly the volume of a mole of condensed gas.

Life's a Gas – now you know more about it.

Yes, read your book. Try some of those problems in the back of the chapter. You'll feel so GOOD about yourself.

Standard Disclaimer

Any mistakes on this review sheet are NOT intentional. You should crosscheck all stated information. You should double-check your book too (see errata).